

Math 122 - #19
Sequences

Find the limit of the following sequences:

1. $\left\{ \left(1 + \frac{1}{n}\right)^n \right\}_{n=1}^{\infty}$

2. $\{3 + (-1)^n\}_{n=1}^{\infty}$

3. $\left\{ \frac{3n^2 - n + 4}{2n^2 + 1} \right\}_{n=1}^{\infty}$

4. $\left\{ \frac{3^n}{4^n} \right\}_{n=1}^{\infty}$

5. $\left\{ n \sin \frac{1}{n} \right\}_{n=1}^{\infty}$

6. $\left\{ \frac{1 + (-1)^n}{n} \right\}_{n=1}^{\infty}$

7. $\left\{ \frac{\sqrt{n}}{1 + \sqrt{n}} \right\}_{n=1}^{\infty}$

8. $\left\{ \frac{n-1}{n} - \frac{n}{n-1} \right\}_{n=2}^{\infty}$

Determine if the following sequences are increasing, decreasing or neither.
Discuss the boundedness of the sequence.

9. $\left\{ 4 - \frac{1}{n} \right\}_{n=1}^{\infty}$

10. $\left\{ \frac{4n}{n+1} \right\}_{n=1}^{\infty}$

11. $\left\{ \frac{\cos n}{n} \right\}_{n=1}^{\infty}$

Answers

1. e

2. D.N.E.

3. $\frac{3}{2}$

4. 0

5. 1

6. 0

7. 1

8. 0

9. Increasing, bounded between 3 and 4

10. Increasing, bounded between 2 and 4

11. Neither, bounded between -1 and 1