	Math 122 Test 2		
SI:	0 4 1 14 2027	EF:	
	October 14, 2025		

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$Name_$		

1	
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Total	

Directions:

- 1. No books, notes or music parts with only one note. You may use a calculator to do routine arithmetic computations. You may *not* use your calculator to store notes or formulas. You may not share a calculator with anyone.
- 2. You should show your work, and explain how you arrived at your answers. A correct answer with no work shown (except on problems which are completely trivial) will receive no credit. If you are not sure whether you have written enough, please ask.
- 3. You may not make more than one attempt at a problem. If you make several attempts, you must indicate which one you want counted, or you will be penalized.
- 4. You may leave as soon as you are finished, but once you leave the exam, you may not make any changes to your exam.

1. (20 points)

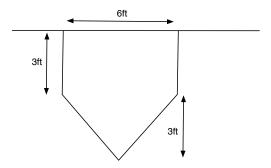
(a) Let p(x)=ax+b for $0\leq x\leq 5$ be a probability density function and have mean $\mu=\frac{35}{12}$

Find the values of a and b.

(b) Find the surface area of the solid of revolution if $y=\sqrt{7-x}$ for $0\leq x\leq 3$ is rotated about the x-axis.

- 2. (20 points)
 - (a) Find the centroid of the region lying between $y=x^2$ and y=0 for $0 \le x \le 2$.

(b) Find the force on the vertical flat plate shown below that is submerged in water (ρ =62.4 lb/ ft³). The top of the plate is at the surface of the water.



3. (20 points)

(a) Solve
$$(x+2)y' = x^2y - 4y;$$
 $y(0) = 3$

(b) Use Euler's method with h = .5 to approximate y(2) if

$$x\frac{dy}{dx} = y^2 + 1 \qquad y(1) = 0$$

- 4. (20 points)
 - (a) Konrad takes his 72° F bagel outside where the temperature is -20° F. At 12:00 PM, the bagel's temperature has dropped to 60° F, and by 12:02 PM, it has cooled further to 50° F. At what time did Konrad originally take the bagel outside?

(b) Typhoid Jonathan has sparked a flu outbreak at CWRU. After one week, 200 students are infected. By the end of the second week, the number of infected students has increased to 500.

$$\frac{dy}{dt} = ky(1 - \frac{y}{A})$$

with carrying capacity of 1000. How many people did Jonathan originally infected?

- 5. (20 points)
 - (a) Solve $x^2y' + 3xy = e^{-x^2}$ y(1) = 0

(b) Vincent is brewing one of his sinister concoctions. He starts with a tank containing 20 gallons of water and 5 ounces of eye-of-newt. A solution with a concentration of 3 ounces of eye-of-newt per gallon flows into the tank at a rate of 4 gallons per minute. At the same time, the well-stirred mixture is draining from the tank at the same rate of 4 gallons per minute. How much eye-of-newt is in the tank after 10 minutes?

FORMULA PAGE

$$\sin^2\theta + \cos^2\theta = 1$$

$$\tan^2\theta + 1 = \sec^2\theta$$

$$1 + \cot^2\theta = \csc^2\theta$$

$$\sin(\alpha + \beta) = \sin\alpha\cos\beta + \cos\alpha\sin\beta$$

$$\sin(\alpha - \beta) = \sin\alpha\cos\beta - \cos\alpha\sin\beta$$

$$\cos(\alpha + \beta) = \cos\alpha\cos\beta - \sin\alpha\sin\beta$$

$$\cos(\alpha - \beta) = \cos\alpha\cos\beta + \sin\alpha\sin\beta$$

$$\tan(\alpha + \beta) = \frac{\tan\alpha + \tan\beta}{1 - \tan\alpha\tan\beta}$$

$$\sin^2 x = \frac{1 - \cos 2x}{2}$$

$$\cos^2 x = \frac{1 + \cos 2x}{2}$$

$$\sin 2x = 2\sin x \cos x$$

$$(\sin x)' = \cos x$$

$$(\cos x)' = -\sin x$$

$$(\tan x)' = \sec^2 x$$

$$(\sec x)' = \sec x \tan x$$

$$(\csc x)' = -\csc x \cot x$$

$$(\cot x)' = -\csc^2 x$$

$$(e^x)' = e^x$$

$$(\ln x)' = \frac{1}{x}$$

$$(\arctan x)' = \frac{1}{x}$$

$$(\arctan x)' = \frac{1}{x}$$

$$(\arctan x)' = \frac{1}{|x|\sqrt{x^2 - 1}}$$

$$\sinh x = \frac{e^x - e^{-x}}{2}$$

$$\cosh x = \frac{e^x + e^{-x}}{2}$$

$$\cosh^2 x - \sinh^2 x = 1$$

$$(\cosh x)' = \sinh x$$

$$(\operatorname{arcsinh} x)' = \frac{1}{\sqrt{x^2 + 1}}$$

$$(\operatorname{arccosh} x)' = \frac{1}{\sqrt{x^2 - 1}}$$

$$(\operatorname{arctanh} x)' = \frac{1}{1 - x^2}$$

$$x_{n+1} = x_n - \frac{f(x_n)}{f'(x_n)}$$

$$f'(c) = \frac{f(b) - f(a)}{b - a}$$

$$f(c) = \frac{1}{b - a} \int_a^b f(x) dx$$

$$\int \sec x \, dx = \ln|\sec x + \tan x| + C$$

$$\int \sec^3 x \, dx = \frac{1}{2} [\sec x \tan x + \ln|\sec x + \tan x|] + C$$

$$\int \csc x \, dx = \ln|\csc x - \cot x| + C$$

$$y' = ky \left(1 - \frac{y}{A}\right)$$

$$y = \frac{A}{1 - \frac{e^{-kt}}{B}} \qquad B = \frac{y_0}{y_0 - A}$$

$$1 + 1 = 2$$

 $(\sinh x)' = \cosh x$