Math 121 Test 1

EF:	

September 20, 2016

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	1.	
Name	KEY	
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Directions:

- 1. No books, notes or Galaxy Note7s. You may use a calculator to do routine arithmetic computations. You may *not* use your calculator to store notes or formulas. You may not share a calculator with anyone.
- 2. You should show your work and explain how you arrived at your answers. A correct answer with no work shown (except on problems which are completely trivial) will receive no credit. If you are not sure whether you have written enough, please ask.
- 3. You may not make more than one attempt at a problem. If you make several attempts, you must indicate which one you want counted, or you will be penalized.
- 4. You may leave as soon as you are finished, but once you leave the exam, you may not make any changes to your exam.
- 5. This test has 7 problems.

1. (20 Points)

(a) Write |3x - 4| < 2 in the form a < x < b.

$$-2 < 3x - 4 < 2$$
 $2 < 3x < 6$
 $2 < x < 2$

(b) Find the equation of the line through (1, -2) and (2, 4)

$$M = \frac{4 - -2}{2 - 1} = 6$$

$$Y + 2 = 6(x - 1) \quad Y + 2 = 6x - 6$$

$$Y = 6x - 8$$

(e) Find the domain of $f(x) = \frac{x + x^{-1}}{(x - 3)(x + 4)}$

(d) If $0 \le \theta \le \pi/2$, find $\sin \theta$, $\cos \theta$ and $\sec \theta$ if $\cot \theta = 4$

$$\begin{array}{c}
\sqrt{7} \\
\sqrt{5} \\
4
\end{array}$$

$$\begin{array}{c}
\sqrt{17} \\
\sqrt{1$$

2. (15 points)

(a) Find
$$f^{-1}(x)$$
 for $f(x) = \frac{1}{2x+1}$

$$(3\lambda+1) = \frac{3\lambda+1}{1}$$

$$\lambda = \frac{3\lambda+1}{1}$$

$$2xy + x = 1$$

$$3xy = 1 - x$$

$$1 = \frac{3x}{1 - x}$$

$$\sqrt{1 - x}$$

(b) Solve for x: $2^{3x+1} = 32$

$$3^{3x+1} = 2^5$$

$$3x+1=5$$

$$x = \frac{4}{3}$$

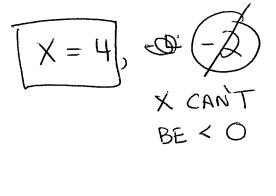
(c) Solve for x: $2 \ln x - \ln(x+4) = \ln 2$

$$\frac{\chi^{2}}{x+4} = 2$$

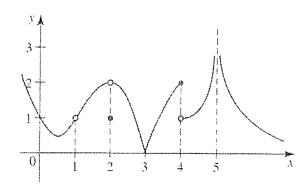
$$\chi^{2} = 2x + 8$$

$$\chi^{2} - 2x - 8 = 0$$

$$(x - 4)(x+2) = 0$$



3. (10 points) Below is the graph of f(x).



Find:

(a)
$$\lim_{x \to 1} f(x)$$

(b)
$$\lim_{x\to 2} f(x) = 2$$

(c)
$$f(2) = 1$$

(d)
$$\lim_{x\to 3} f(x) = \bigcirc$$

(e)
$$\lim_{x \to 4^-} f(x) = 2$$

(f)
$$\lim_{x \to 4^+} f(x) =$$

(g)
$$\lim_{x\to 4} f(x) = D.NE$$
.

$$_{(h)} f(4) = 2$$

(i)
$$\lim_{x \to 5} f(x) = +\infty$$

 0 NE

(a)
$$\lim_{x \to 1} \frac{5 - x^2}{4x + 7}$$

$$=\frac{5-1}{4+7}=\boxed{\frac{4}{11}}$$

(b)
$$\lim_{x\to 0} \frac{e^{3x} - e^x}{e^x - 1} = 0$$
 $(e^{X} + 1)$ $(e^{X} + 1)$

(c)
$$\lim_{a\to b} \frac{a^2 - 3ab + 2b^2}{a - b} = 2mm$$
 (ab) (a-2b)

$$=b-ab=\overline{-b}$$

(d)
$$\lim_{s \to 0} \frac{1 - \sqrt{s^2 + 1}}{s^2} \left(\frac{1 + \sqrt{5^2 + 1}}{1 + \sqrt{5^2 + 1}} \right)$$

$$= \lim_{s \to 0} \frac{x - (s^2 + 1)}{s^2 (1 + (s^2 + 1))} = \boxed{\frac{-1}{2}}$$

5. (15 points)

(a) Find the value of a and b so that f(x) is continuous if

$$ax + b = 4$$

$$2ax - b = 4$$

$$3a = 8$$

$$0 + b = 4$$

$$2ax - b = 4$$

$$3a = 8$$

$$0 = 8$$

$$0 = 8$$

$$0 = 8$$

$$0 = 8$$

$$0 = 8$$

$$0 = 8$$

$$0 = 8$$

$$0 = 8$$

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$$0 = 8$$

$$0 = 8$$

(b)
$$\lim_{x\to 0} \frac{1-\cos 3x}{3x^2} \sim \frac{1+\cos 3x}{1+\cos 3x}$$

$$= 2 m \frac{1 - \cos^2 3x}{3x^2 (1 + \cos 3x)}$$

$$= 2 m \frac{51N3x}{3x} \frac{51N3x}{3x} \cdot \frac{3}{(1 + \cos 3x)} = \boxed{\frac{3}{2}}$$

$$\times \Rightarrow 0$$

(c)
$$\lim_{x \to -\infty} \frac{4x^2 - 3}{\sqrt{25x^4 + 4x + 200}}$$

$$=$$
 $\begin{bmatrix} \frac{4}{5} \end{bmatrix}$

6. (10 points) Show that
$$\sqrt{x} + \sqrt{x+2} = 3$$
 has a solution.

$$f(x) = \sqrt{x} + \sqrt{x+2} \qquad f(x) \text{ is cont.}$$

$$f(0) = \sqrt{2} \cdot 2 \cdot 1.41$$

$$f(2) = \sqrt{2} + 2 \cdot 2 \cdot 3.14$$

$$\text{SINCE } 1.41 < 3 < 3.14$$

$$\text{BY THE IVT THERE IS A C}$$

$$\text{SO THAT } f(C) = 3$$

7. (10 points) Indicate whether the following statements are true or false by circling the appropriate letter. A statement which is sometimes true and sometimes false should be marked false.

a) If
$$\lim_{x\to 3} f(x) = L$$
, then $L = f(3)$.

b) If
$$\lim_{x \to 0} \frac{f(x)}{x} = 1$$
, then $f(0) = 0$ **T**

c) If
$$\lim_{x \to -7} f(x) = 8$$
 then $\lim_{x \to -7} \frac{8}{f(x)} = 1$ **T**

d) If
$$\lim_{\substack{x\to 5^+\\ x\to 5^+\\ x\to 5}} f(x)=4$$
 and $\lim_{\substack{x\to 5^-\\ x\to 5^-}} f(x)=2$ then T

e) If
$$\lim_{x\to 2} f(x) = 2$$
 then $\lim_{x\to 4} f(x) = 4$ T