## Math 121 Test 1

EF:

## September 16, 2014

1	
2,	
3	
4	g
5	
6	
Total	6

Name KEY

## Directions:

- 1. No books, notes or yik yakking about your SI. You may use a calculator to do routine arithmetic computations. You may not use your calculator to store notes or formulas. You may not share a calculator with anyone.
- 2. You should show your work, and explain how you arrived at your answers. A correct answer with no work shown (except on problems which are completely trivial) will receive no credit. If you are not sure whether you have written enough, please ask.
- 3. You may not make more than one attempt at a problem. If you make several attempts, you must indicate which one you want counted, or you will be penalized.
- 4. You may leave as soon as you are finished, but once you leave the exam, you may not make any changes to your exam.
- 5. This test has 6 problems.

- 1. (20 Points)
  - (a) Write |2x + 1| < 5 in the form a < x < b.

$$-3 < x < 2$$

(b) Find the equation of the line with x-intercept x=4 and y intercept y=3.

$$y = mx + 3$$

$$m = -\frac{3}{4}$$

(c) Find the domain of  $f(x) = \frac{x + x^{-1}}{(x - 3)(x + 4)}$ 

$$=\frac{X+\frac{1}{X}}{(X-3)(X+4)}$$

 $Y = -\frac{3}{4}x + 3$ 

(d) Find  $\cos \theta$  and  $\tan \theta$  if  $\cot \theta = \frac{4}{3}$  and  $\sin \theta < 0$ .

$$\cos\theta = \frac{-4}{5}$$

$$TANG = \frac{3}{4}$$

(a) Let 
$$f(x) = \sqrt{2 - x^2}$$
 and  $g(x) = \frac{1}{2 - x}$ , find i.  $(f \circ g)(x)$ 

$$f(g(x)) = f\left(\frac{1}{a-x}\right) = \sqrt{2 - \left(\frac{1}{a-x}\right)^2}$$

ii. 
$$(g \circ f)(x)$$

$$g(t(x)) = g(\sqrt{2-x^2}) = \frac{1}{2-(\sqrt{2-x^2})}$$

(b) Find the exact value of  $\cosh(3 \ln 2)$ 

$$= \frac{2 \ln 2}{2} - 3 \ln 2 = \frac{\ln 8}{2} = \frac{\ln 8}{2} = \frac{\ln 8}{2} = \frac{16}{16}$$

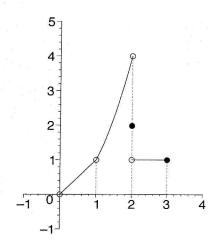
(c) Solve for x:  $\log_3 x + 3\log_3(x^2) = 14$ 

$$LoG_3(x^7) = 14$$
  $3^{14} = x^7$   
 $X = 3^7$   $X = 9$ 

(d) Solve for  $x: 7^{x+1} = (\frac{1}{7})^{2x}$ 

$$\begin{array}{r}
 7^{X+1} = 7^{2X} \\
 \hline
 3X = -1 \\
 \boxed{X = -\frac{1}{3}}
 \end{array}$$

3. (10 points) Below is the graph of f(x).



Find:

(a) 
$$\lim_{x \to 0^+} f(x)$$
 = 0

(b) 
$$\lim_{x \to 1} f(x)$$
 = 1

(c) 
$$\lim_{x \to 2^{-}} f(x) = 4$$

(d) 
$$\lim_{x\to 2^+} f(x)$$
 :=

(e) 
$$f(2)$$
  $=$   $2$ 

4. (20 points)

(a) 
$$\lim_{x \to -1} \frac{x^2 + 1}{(x^3 + 2)(x^4 + 1)} = \frac{2}{3} = 1$$

(b) 
$$\lim_{x\to 2} \frac{x^2 - 4x + 4}{x^2 + x - 6} = \lim_{X\to 2} \frac{(x-2)(x-3)}{(x-3)(x+3)} = 0$$

(c) 
$$\lim_{x \to 1} \left( \frac{1}{x-1} - \frac{2}{x^2-1} \right) = 0$$
  $(x^2-1) - \lambda(x-1)$ 

$$= \lim_{x \to 1} \frac{(x+1)^2}{(x+1)(x+1)} = \frac{1}{2}$$

(d) 
$$\lim_{h\to 5} \frac{h-5}{\sqrt{h+4}-3} \left( \frac{\sqrt{h+4}+3}{\sqrt{h+4}+3} \right)$$

## 5. (20 points)

(a) Find the value of a and b so that f(x) is continuous if

$$f(x) = \begin{cases} ax+b & x < 1 \\ 4 & x = 1 \\ 2ax-b & x > 1 \end{cases}$$

$$0.+b=4$$

$$2a-b=4$$

$$3\alpha = 8$$

$$\alpha = \frac{8}{3} \quad b = \frac{4}{3}$$

(b) 
$$\lim_{x\to 0^{+}} \sqrt{x} e^{\cos(\pi/x)} = 0$$

$$-1 \leq \cos\left(\frac{\pi}{x}\right) \leq 1$$

$$e^{-1} \leq e^{\cos\left(\frac{\pi}{x}\right)} \leq e$$

$$\sqrt{x} e^{-1} \leq \sqrt{x} e^{\cos\left(\frac{\pi}{x}\right)} \leq e$$
(c)  $\lim_{x\to -\infty} \frac{\sqrt{2x^{2}+3}}{3x-6}$ 

(d) 
$$\lim_{x\to 0^+} \frac{\sqrt{1-\cos x}}{x} \left(\frac{\sqrt{1+\cos x}}{\sqrt{1+\cos x}}\right) = \lim_{X\to 0^+} \frac{\sqrt{1-\cos^2 x}}{x \left(\sqrt{1+\cos x}\right)}$$

$$= \lim_{x \to 0^+} \frac{\sin x}{x} \frac{1}{\sqrt{1+\cos x}} = \frac{1}{\sqrt{2}}$$

6. (10 points) Indicate whether the following statements are true or false by circling the appropriate letter. A statement which is sometimes true and sometimes false should be marked false.

a) 
$$\lim_{x\to 3^-} f(x) = 2, \text{ and } \lim_{x\to 3^+} f(x) = 2 \text{ then}$$
$$\lim_{x\to 3} f(x) = 2.$$
 T

b) If 
$$\lim_{x\to 2^-} f(x) = 3$$
, and  $\lim_{x\to 2^+} f(x) = 4$  then  $f(2)$  must equal 3 or 4.

c) 
$$\sin(\arctan x) = \frac{x}{\sqrt{1+x^2}}$$
. T

d) If 
$$f(1) = -2$$
 and  $f(2) = 4$ , then  $f(c) = 0$  for some  $1 \le c \le 2$ .

e) If 
$$f(x) = \frac{x+1}{x-1}$$
 then  $f^{-1}(x) = \frac{x+1}{x-1}$ .