Math 121 Test 1

EF:

September 17, 2013

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Directions:

- 1. No books, notes or asbestos. You may use a calculator to do routine arithmetic computations. You may *not* use your calculator to store notes or formulas. You may not share a calculator with anyone.
- 2. You should show your work, and explain how you arrived at your answers. A correct answer with no work shown (except on problems which are completely trivial) will receive no credit. If you are not sure whether you have written enough, please ask.
- 3. You may not make more than one attempt at a problem. If you make several attempts, you must indicate which one you want counted, or you will be penalized.
- 4. You may leave as soon as you are finished, but once you leave the exam, you may not make any changes to your exam.
- 5. This test has 7 problems.

1. (15 Points)

(a) Find the domain of
$$f(x) = \frac{\sqrt{2-x}}{\sqrt{4-x^2}}$$

$$4 - x^{2} > 0$$
 $4 - x^{2} = 0$
 $4 - x^{2} =$

(b) Find x such that (x, 4) is on the line with slope m = -3 that goes through the point (-2, 13).

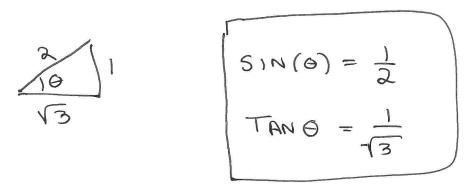
$$Y - 13 = -3(x+2)$$

$$4 - 13 = -3(x+2)$$

$$-9 = -3(x+2)$$

$$3 = x+2$$
 $X = 1$

(c) Find $\sin \theta$ and $\tan \theta$ if $\csc \theta = 2$ and $0 < \theta < \pi/2$.



2. (20 points)

(a) Which of the following is equal to
$$sec(arcsin x)$$
?

a)
$$\frac{1}{\sqrt{1+x^2}}$$

b)
$$\frac{\sqrt{1-x^2}}{x}$$

c)
$$\frac{x}{\sqrt{1-x^2}}$$

Which of the following is equal to
$$sec(\arcsin x)$$
?

a) $\frac{1}{\sqrt{1+x^2}}$ b) $\frac{\sqrt{1-x^2}}{x}$ c) $\frac{x}{\sqrt{1-x^2}}$ d) $\frac{1}{\sqrt{1-x^2}}$

(b) Find
$$f^{-1}(x)$$
 for $f(x) = \frac{3x+2}{5x-1}$ $y = \frac{3x+2}{5x-1}$

$$Y = \frac{3x+2}{5x-1}$$

$$X = \frac{3Y+2}{5Y-1}$$
 $(5Y-1)(x) = 3Y+2$ $Y(5X-3) = X+2$

$$(5Y-1)(x) = 3y+2$$

$$5xy-x=3y+2$$

$$5xy - 3y = x + 2$$

$$5xy - 3y = x + 2$$
 $y = x + 2$
 $y = x + 2$

(c) Solve for
$$x$$
: $e^{2x} + e^x = 12$

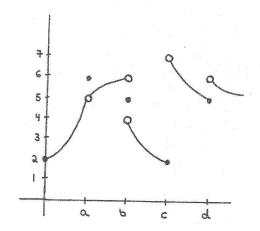
$$e^{3x} + e^{x} - 12 = 0$$

$$e^{\lambda} = 3$$

$$en(e^{x}) = ln 3$$

(d) Simplify
$$10\log_b(b^3) - 4\log_b(\sqrt{b})$$

3. (10 points) Below is the graph of f(x).



Find:

(a)
$$\lim_{x \to a} f(x) = 5$$

(b)
$$\lim_{x\to b} f(x) = DN \in$$

(c)
$$\lim_{x \to c^-} f(x) = 2$$

(d)
$$\lim_{x \to d^+} f(x) = \mathcal{C}$$

(e)
$$f(b) = 5$$

(a)
$$\lim_{x \to 1} \frac{5 - x^2}{4x + 7} = \frac{1}{11}$$

(b)
$$\lim_{x \to 2} \frac{2^{2x} + 2^x - 20}{2^x - 4} = \lim_{x \to 2} \frac{(2^x + 4)(2^x + 5)}{(2^x + 5)}$$

$$= 9$$

(c)
$$\lim_{x \to 3^{-}} \frac{\sqrt{x^2 - 6x + 9}}{x - 3} - \lim_{x \to 3^{-}} \frac{\sqrt{(x - 3)^2}}{x - 3}$$

$$= \lim_{X \to 3} \frac{|x-3|}{x-3} = \lim_{X \to 3} -(x-3) = -1$$

(d)
$$\lim_{x \to 8} \frac{\sqrt{x+1} - 3}{x - 8}$$
 $\frac{\sqrt{x+1} + 3}{\sqrt{x+1} + 3}$

5. (15 points)

(a) Find the value of a and b so that f(x) is continuous if

$$f(x) = \begin{cases} x^{-1} & x < -1 \\ ax + b & -1 \le x \le \frac{1}{2} \\ x^{-1} & x > \frac{1}{2} \end{cases} \qquad 2x + 1$$

$$a(-1) + b = -1$$
 $a(\frac{1}{2}) + b = 2$
 $\frac{3}{2}a = 3$
 $a = 2$
 $b = 1$

(b) $\lim_{x \to 0} \frac{(\sin 5x)(\sin 4x)}{(\sin 3x)(\sin 2x)}$

=
$$\frac{1}{20} = \frac{10}{6} = \frac{10}{3}$$

(c)
$$\lim_{x \to -\infty} \frac{4x - 3}{\sqrt{25x^2 + 4x}} = -\frac{4}{5}$$

- 6. (10 points) To show that $\lim_{x\to 5} x^2 = 25$
 - (a) Show that if 4 < x < 6 then $|x^2 25| < 11 |x 5|$.

$$|x^2-25| = |(x-5)(x+5)|$$
 q < 11 |x-5|
x+5<11 IF x<6

(b) Find δ such that if $0 < |x - 5| < \delta$ then $|x^2 - 25| < .001$

$$|x^2-a5| = |x-5| \times |$$

(c) Find δ such that if $0 < |x - 5| < \delta$ then $|x^2 - 25| < \epsilon$

$$|x^{2}-25| \leq |(x-5)(x+5)| < 11|x-5| < \epsilon$$

$$|x-5| < \frac{\epsilon}{11}$$

- 7. (10 points) Indicate whether the following statements are true or false by circling the appropriate letter. A statement which is sometimes true and sometimes false should be marked false.
 - a) If f(x) is continuous at x = c then $(f(x))^2$ is continuous at x = c.

b) If
$$\lim_{x \to c} f(x) = L$$
, then $\frac{\lim_{x \to c^{-}} f(x)}{\lim_{x \to c^{+}} f(x)} = 1$

c) If
$$f(x) \neq g(x)$$
 for all $x \neq c$, then
$$\lim_{x \to c} f(x) \neq \lim_{x \to c} g(x)$$

When using the bisection method to find where d)
$$f(x) = 0$$
, if $f(1) = 2$ and $f(2) = 9$, then $f(x) \neq 0$ for all $1 \leq x \leq 2$

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e) If
$$f(x)$$
 is a polynomial and $f(1) = -2$ and $f(4) = 5$, then there is a c with $1 < c < 4$ where $f(c) = 0$

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