Quiz Book Number	Math 121 Test 3	EF:
	November 19, 2024	
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	1
Name.	2
	3
	4
	5
	Total

Directions:

- 1. No books, notes or unicycle TikTok videos. You may use a calculator to do routine arithmetic computations. You may *not* use your calculator to store notes or formulas. You may not share a calculator with anyone.
- 2. You should show your work, and explain how you arrived at your answers. A correct answer with no work shown (except on problems which are completely trivial) will receive no credit. If you are not sure whether you have written enough, please ask.
- 3. You may not make more than one attempt at a problem. If you make several attempts, you must indicate which one you want counted, or you will be penalized.
- 4. You may leave as soon as you are finished, but once you leave the exam, you may not make any changes to your exam.
- 5. This test has 5 problems.

- 1. (20 points)
 - (a) Use a linear approximation to estimate $\sqrt[5]{33}$.

(b) Find the maximum and minimum values for $f(x) = x^2 - 8 \ln x$ on the interval [1, 4]

(c) If using Newton's Method to find where

$$4 + 8x^2 - x^4 = 0$$

Circle which of the following that would NOT be a good place to start Newton's Method (there may be more than one)?

- i) x = -3 ii) x = -2 iii) x = -1 iv) x = 0

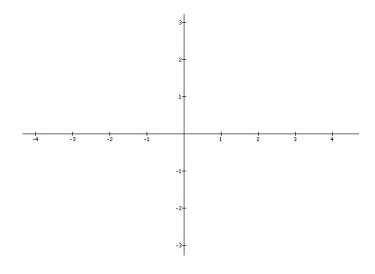
- v) x = 1 vi) x = 2 vii) x = 3

2. (20 points) For $f(x) = \frac{x}{x^2 - 4}$

Hint:
$$f'(x) = -\frac{x^2 + 4}{(x^2 - 4)^2}$$
 and $f''(x) = \frac{2x(x^2 + 12)}{(x^2 - 4)^3}$

find:

- (a) Domain:
- (b) Range:
- (c) x-intercepts:
- (d) y-intercepts:
- (e) Where y is increasing:
- (f) Where y is decreasing:
- (g) Critical points:
- (h) Where y is concave up:
- (i) Where y is concave down:
- (j) Inflection points:
- (k) Vertical asymptotes:
- (l) Horizontal asymptotes:
- (m) Sketch the graph of y

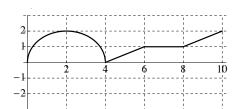


- 3. (20 points)
 - (a) Chez Bútler, a very fancy restaurant, is trying to decide how much to charge per seat for reservations on Thanksgiving. Experience has shown that at a cost of \$200 per seat, all 80 seats in the restaurant will be booked. On average, there will be one fewer customer for each \$20 increase in price above \$200. What price should be charge to maximize revenue?

(b) Compute
$$\lim_{x\to 0} \frac{e^x + e^{-x} - 2}{1 - \cos x}$$

(c) Find $\lim_{x \to \pi/4} (1 - \tan x) \sec 2x$

- 4. (20 points)
 - (a) The graph of a piecewise defined function f(x) consisting of a semicircle and 3 straight lines, is shown below.



i. Use the graph to calculate the value of R_5 , the right endpoint approximation to $\int\limits_0^{10} f(x) \ dx$ using 5 equal subintervals

ii. Compute $\int_{0}^{10} f(x) dx$

(b) Konrad was writing a question for this test. The answer was

$$\int f(x) \ dx = e^x \arctan x + C$$

but he can't remember what f(x) was supposed to be. Please help Konrad and find f(x)

5. (20 points)

(a) Compute:
$$\int (4-3x^2)(4x+1) dx$$

(b) Compute
$$\int x^2 \sqrt{x-1} \ dx$$

(c) Compute:
$$\int_{0}^{\sqrt{\pi}} x \sin(x^2) dx$$

(d) Compute
$$\int \frac{\sec^2 x}{\sqrt{1-\tan^2 x}} dx$$

FORMULA PAGE

$$\sin^2\theta + \cos^2\theta = 1$$

$$\tan^2\theta + 1 = \sec^2\theta$$

$$1 + \cot^2\theta = \csc^2\theta$$

$$\sin(\alpha + \beta) = \sin\alpha\cos\beta + \cos\alpha\sin\beta$$

$$\sin(\alpha - \beta) = \sin\alpha\cos\beta - \cos\alpha\sin\beta$$

$$\cos(\alpha + \beta) = \cos\alpha\cos\beta - \sin\alpha\sin\beta$$

$$\cos(\alpha - \beta) = \cos\alpha\cos\beta + \sin\alpha\sin\beta$$

$$\tan(\alpha + \beta) = \frac{\tan\alpha + \tan\beta}{1 - \tan\alpha\tan\beta}$$

$$\sin^2 x = \frac{1 - \cos 2x}{2}$$

$$\cos^2 x = \frac{1 + \cos 2x}{2}$$

$$\sin 2x = 2\sin x \cos x$$

$$\cos 2x = \cos^2 x - \sin^2 x$$

$$(\sin x)' = \cos x$$

$$(\cos x)' = -\sin x$$

$$(\tan x)' = \sec^2 x$$

$$(\sec x)' = \sec x \tan x$$

$$(\csc x)' = -\csc x \cot x$$

$$(\cot x)' = -\csc^2 x$$

$$(e^x)' = e^x$$

$$(\ln x)' = \frac{1}{x}$$

$$(\operatorname{arcsin} x)' = \frac{1}{|x|\sqrt{x^2 - 1}}$$

$$(\sinh x)' = \cosh x$$

$$(\cosh x)' = \sinh x$$

$$\sinh x = \frac{e^x - e^{-x}}{2}$$

$$\cosh x = \frac{e^x + e^{-x}}{2}$$

$$x_{n+1} = x_n - \frac{f(x_n)}{f'(x_n)}$$

$$f'(c) = \frac{f(b) - f(a)}{b - a}$$

$$\sum_{j=1}^n j = \frac{n(n+1)}{2}$$

$$\sum_{j=1}^n j^2 = \frac{n(n+1)(2n+1)}{6}$$

$$\sum_{j=1}^n j^3 = \left[\frac{n(n+1)}{2}\right]^2$$

$$\Delta x = \frac{b-a}{n}$$

$$x_j = a + j\Delta x$$

$$\int_a^b f(x)dx = \lim_{n \to \infty} \sum_{j=1}^n f(x_j)\Delta x$$

$$1 + 1 = 2$$