Math 122 Quiz 11 Review

1. For
$$\vec{a} = \langle 2, 1, 1 \rangle$$
 and $\vec{b} = \langle 1, -1, -1 \rangle$, find $\vec{a} \times \vec{b}$.

2. For
$$\vec{a} = \langle 1, -1, 0 \rangle$$
 and $\vec{b} = \langle 1, 1, 0 \rangle$, find $\vec{a} \times \vec{b}$.

3. For
$$\vec{a} = \langle 3, -4, 1 \rangle$$
 and $\vec{b} = \langle 2, -2, 3 \rangle$, find $\vec{a} \times \vec{b}$.

4. If
$$\langle -1, 3, 5 \rangle \times \langle 0, a, 1 \rangle = \langle -2, 1, -1 \rangle$$
, what is a ?

- **5.** Find two unit vectors perpendicular to both $\vec{a} = \langle 1, 2, 1 \rangle$ and $\vec{b} = \langle 3, -4, 2 \rangle$.
- **6.** Find two unit vectors perpendicular to both $\overrightarrow{a} = \langle 1, 2, 3 \rangle$ and $\overrightarrow{b} = \langle -1, 0, 1 \rangle$.
- 7. Find the area of the parallelogram spanned by the vectors $\vec{a}=\langle 3,-3,1\rangle$ and $\vec{b}=\langle -4,9,2\rangle$.
- 8. Find the area of the parallelogram with vertices: (0,-1),(3,4),(1,6) and (-2,1)
- **9.** Find the area of the triangle with vertices A(1,2,3), B(6,4,7), and C(1,5,2).
- **10.** Compute $||\vec{u} \times \vec{v}||$ if $||\vec{u}|| = 2$ and $||\vec{v}|| = 5$ and the angle between \vec{u} and \vec{v} is $\theta = \frac{\pi}{6}$.

11. Let
$$\vec{a} = \langle 3, -4, 0 \rangle$$
, $\vec{b} = \langle 1, -2, 2 \rangle$, and $\vec{c} = \langle 1, -1, 0 \rangle$; find $\vec{c} \cdot (\vec{a} \times \vec{b})$.

12. If
$$\overrightarrow{A} \times \overrightarrow{B} = \overrightarrow{A} \times \overrightarrow{C}$$
 and $\overrightarrow{A} \neq \overrightarrow{0}$ does $\overrightarrow{B} = \overrightarrow{C}$

Answers

1.
$$\vec{a} \times \vec{b} = \langle 0, 3, -3 \rangle$$

2.
$$\vec{a} \times \vec{b} = \langle 0, 0, 2 \rangle$$

3.
$$\vec{a} \times \vec{b} = \langle -10, -7, 2 \rangle$$

4.
$$a = 1$$

5.
$$\pm \frac{1}{\sqrt{165}} \langle 8, 1, -10 \rangle$$

6.
$$\pm \frac{1}{\sqrt{6}} \langle 1, -2, 1 \rangle$$

7.
$$5\sqrt{22}$$

9.
$$\frac{1}{2}\sqrt{446}$$